

# Freshmen Programming Contests 2025

Solutions presentation

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By the Freshmen Programming Contests 2025 jury for:

- AAPJE in Amsterdam
- FPC in Delft
- FYPC in Eindhoven
- GAPC in Groningen
- Contest in Mons

May 3, 2025



Please do not post the problems online

Other universities will have their contests in the coming weeks.

Please, do not post/discuss the problems online before

Saturday 17 May 2025 at 17:00

# G: Gambler's Dilemma

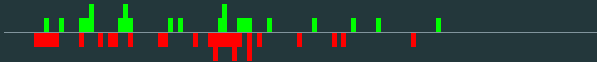
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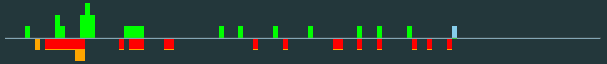
**Pitfall:** Be careful of off-by-one errors when calculating the rank of a card.

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Statistics: 54 submissions, 23 accepted

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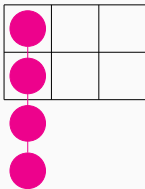


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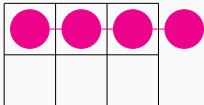


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Statistics: 49 submissions, 21 accepted, 1 unknown



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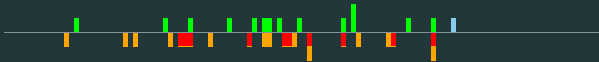
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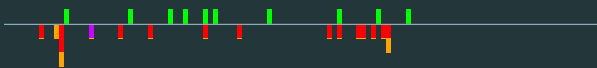
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- If the original  $a_1, \dots, a_n$  satisfied condition, one can select  $\delta$  such that  $a_2 - a_1, a_3 - \delta, a_4, \dots, a_n$  satisfies the condition.

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Statistics: 28 submissions, 10 accepted

## E: Equation Extrapolation

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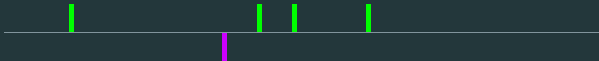


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# F: Frog and Princess

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**Observation 3:** Arbitrary integers  $b_1, b_2, \dots, b_k$  can form a polygon iff

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$$2 \cdot \max(b_1, b_2, \dots, b_k) \leq b_1 + b_2 + \dots + b_k$$

**Solution:** Calculate prefix maximums and prefix sums of array  $a_i$ . For each prefix of length  $k$  from 1 to  $n$ , check the polygon condition and output “yes” if any of the checks succeed.

# F: Frog and Princess

Problem author: Wietze Koops



**Problem:** Given positions of frog and princess, find out if the frog can jump to the princess within  $n$  jumps. The  $i$ th jump should jump a distance of  $a_i$ .

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Fixes: Use `long double` in C++, or `BigInteger` in Java, or rewrite the polygon formula to use  $d(f, p)^2$ , which is an integer:

$$d(f, p) \leq x \iff x \geq 0 \wedge d(f, p)^2 \leq x^2$$

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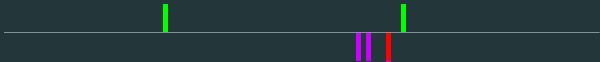
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Statistics: 14 submissions, 3 accepted

# K: Kite Construction

Problem author: Jeroen Op de Beek



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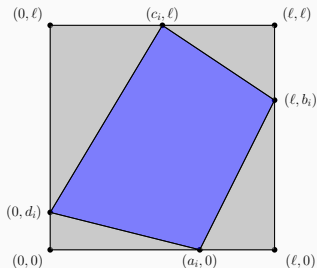
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**Solution:** Let  $(a_i, 0)$ ,  $(\ell, b_i)$ ,  $(c_i, \ell)$  and  $(0, d_i)$  be the coordinates of the corners of the  $i$ th quadrilateral. Then we can compute the sum of the areas by considering how much is cut off from the full  $\ell \times \ell$  square:

$$\sum_{i=1}^n \left( \ell^2 - \frac{1}{2}a_id_i - \frac{1}{2}(\ell - a_i)b_i - \frac{1}{2}(\ell - b_i)(\ell - c_i) - \frac{1}{2}c_i(\ell - d_i) \right).$$



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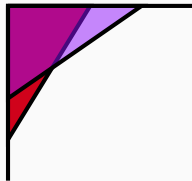
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$$a_i d_j + a_j d_i = a_i d_i + a_j d_j + \underbrace{(a_i - a_j)}_{>0} \underbrace{(d_j - d_i)}_{<0},$$

so swapping  $d_i$  and  $d_j$  would lead to a smaller area cut off.

Hence, whenever  $i < j$  we have  $d_i > d_j$ .



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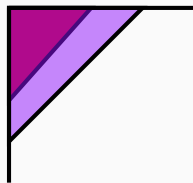
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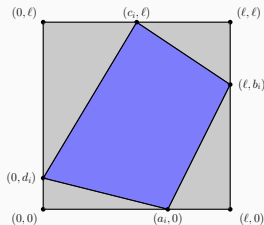
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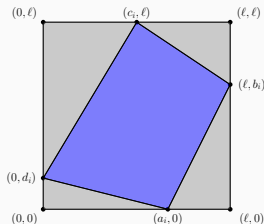
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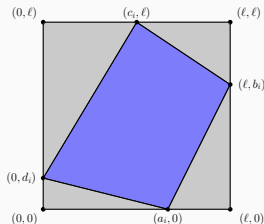
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Statistics: 5 submissions, 2 accepted

# D: Delicious Trees

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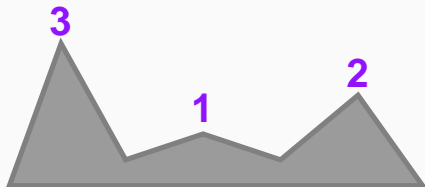
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Statistics: 5 submissions, 1 accepted, 1 unknown

# I: Interesting Mountains

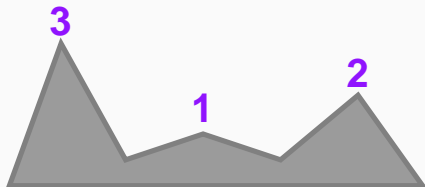
Problem author: Mihail Bankov



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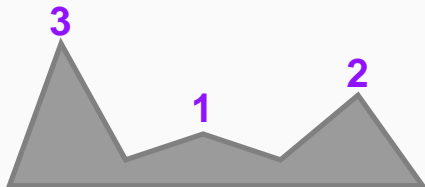
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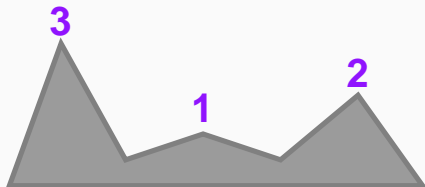
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Let's first learn how to count **inversions**.

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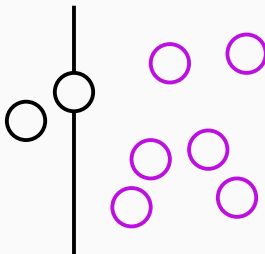
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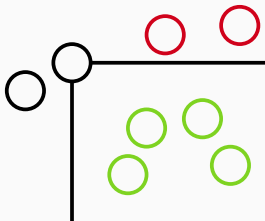
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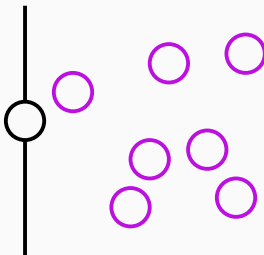
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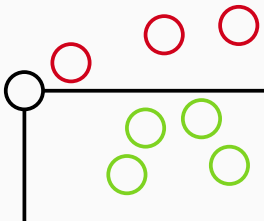
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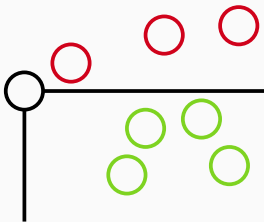
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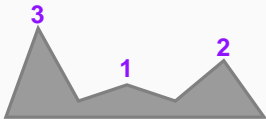
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Using Fenwick tree or segment tree,  $\mathcal{O}(\log(n))$  per query / update.

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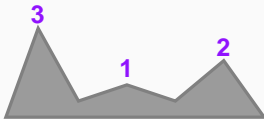


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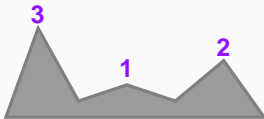
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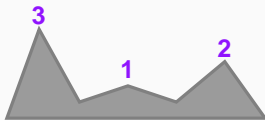
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Statistics: 9 submissions, 0 accepted, 1 unknown

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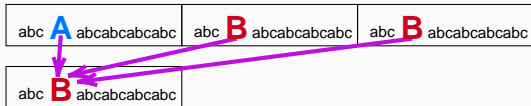
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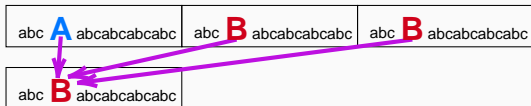
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- Then count how many letters we must have changed.

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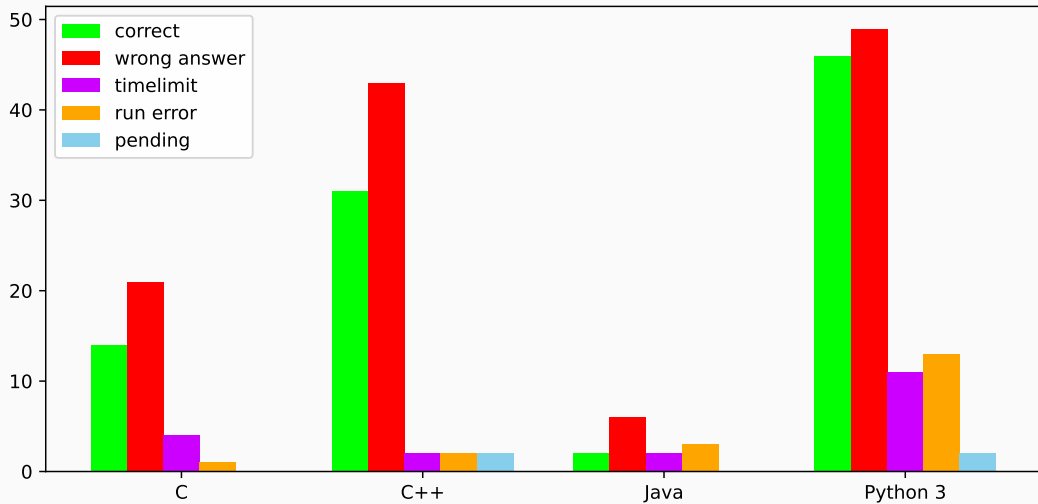
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Statistics: 1 submissions, 0 accepted

## Language stats



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## Random facts

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- The minimum<sup>1</sup> number of lines the jury needed to solve all problems is

$$2 + 1 + 6 + 5 + 1 + 5 + 2 + 2 + 6 + 3 + 6 = 39$$

On average 3.5 lines per problem, down from 6.0 last year

---

<sup>1</sup>After codegolfing

## Thanks to the proofreaders:

- Arnoud van der Leer (TU Delft)
- Dany Sluijk (TU Delft)
- Davina van Meer (Delft)
- Mattia Marziali (RU Groningen)
- Michael Zündorf   
(KIT Karlsruhe / NWERC jury)
- Pavel Kunyavskiy (JetBrains Amsterdam)
- Pierre Vandenhove (UMons)
- Thomas Verwoerd  
(TU Delft,  Kotlin Hero )
- Thore Husfeldt (ITU Copenhagen / BAPC Jury)
- Wendy Yi (KIT Karlsruhe / NWERC jury)

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- Alice Sayutina (VU Amsterdam)
- Angel Karchev (TU Delft)
- Bálint Kollmann (TU Delft)
- Jeroen Op de Beek (TU Delft)
- Leon van der Waal (TU Delft)
- Liudas Staniulis (VU Amsterdam)
- Maarten Sijm (TU Delft)
- Mihail Bankov (TU Delft)
- Moham Balfakeih (TU Delft)
- Wietze Koops (Radboud Nijmegen / RU Groningen)





Want to solve the problems you could not finish?  
Or have friends that like to solve algorithmic problems?

<https://fpcs2025.bapc.eu/>

Saturday 17 May 2025 13:00–17:00

Please, do not post/discuss the problems online before this time!

Excited to participate in the next contest?

Register for the BAPC Preliminaries in September!

Want to organize these contests?

Join the organizing committee!

Want to create programming problems for FPCs next year?

Either join the committee, or contact Maarten Sijm